

Module 2.7 Estimation of uncertainties

Module developers:

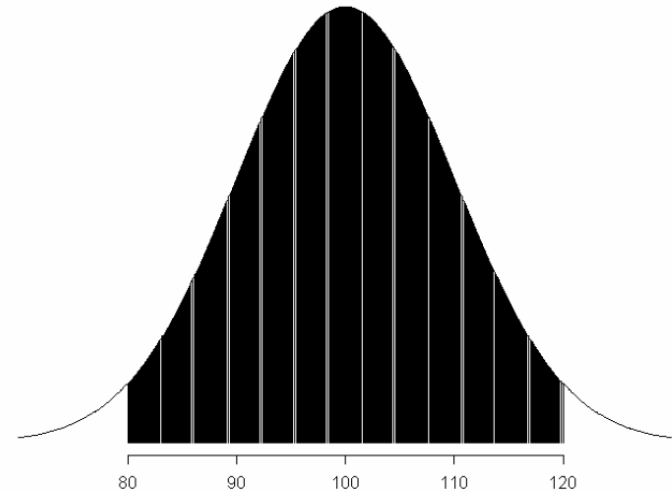
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Source: IPCC GPG LULUCF

After the course the participants should be able to:

- Identify sources of uncertainty in the estimates of area change (activity data) and carbon stocks change (emission factor)
- Implement the correct steps to calculate uncertainties for estimates in area change and carbon stock change
- Understand the possible treatment of uncertainties in a conservative way

V2, December 2016

Background material

- GOFC-GOLD. 2014. *Sourcebook*. Section 2.7.
- IPCC. 2003. *Good Practice Guidance for Land Use, Land-Use Change, and Forestry*. Ch. 5.2, "Identifying and Quantifying Uncertainties."
- IPCC. 2006. *2006 IPCC Guidelines for National Greenhouse Gas Inventories*, vol. 1, ch. 3, "Uncertainties."
- GFOI. 2014. *Integrating Remote-sensing and Ground-based Observations for Estimation of Emissions and Removals of Greenhouse Gases in Forests: Methods and Guidance from the Global Forest Observation Initiative (MGD)*. Sections 3.7 and 4.



Outline of lecture

1. Importance of identifying uncertainties
2. General concepts
3. Uncertainties in area-change estimates
4. Uncertainties in carbon stocks change estimates
5. Combination of uncertainties



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Uncertainty in IPCC and UNFCCC context

- **Uncertainty is the lack of knowledge of the true value of a parameter** (e.g., area and carbon stock estimates in REDD+ context)
- Assessing uncertainty is fundamental in the IPCC and UNFCCC contexts: the IPCC defines greenhouse gas (GHG) inventories consistent with “good practice” as those which “contain neither over- nor underestimates so far as can be judged, and in which uncertainties are reduced as far as practicable.”



Importance of identifying uncertainties

- A correct identification and quantification of the various sources of uncertainty helps to assess the robustness of any GHG inventory (including REDD+ estimates) and prioritize efforts for their further development.
- In the accounting context, information on uncertainty can also be used to develop *conservative* REDD+ estimates, to ensure that reductions in emissions or increases in removals are not overestimated.



Aim of this module: Uncertainty estimation

- Building on the IPCC (2003) guidance, this module aims to provide some basic elements for the *identification*, *quantification*, and *combination* of uncertainties for the estimates of:
 - Area and area changes (the **activity data, AD**)
 - Carbon stocks and carbon stock changes (the **emission factors, EF**)



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Systematic errors and random errors (1/2)

■ **Uncertainty** consists of two components:

- *Bias or systematic error* (lack of *accuracy*) occurs, e.g., due to flaws in the measurements or sampling methods or due to use of an EF that is not suitable
- *Random error* (lack of *precision*) is a random variation above or below a mean value. It cannot be fully avoided but can be reduced by, for example, increasing the sample size.

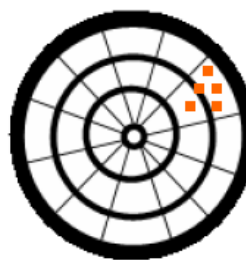
Accuracy: agreement between estimates and exact or true values

Precision: agreement among repeated measurements or estimates

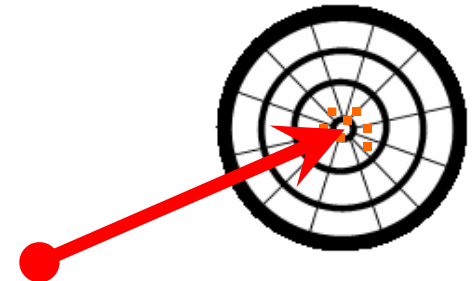
(A) Accurate but not precise



(B) Precise but not accurate



(C) Accurate and precise



Systematic errors and random errors (2/2)

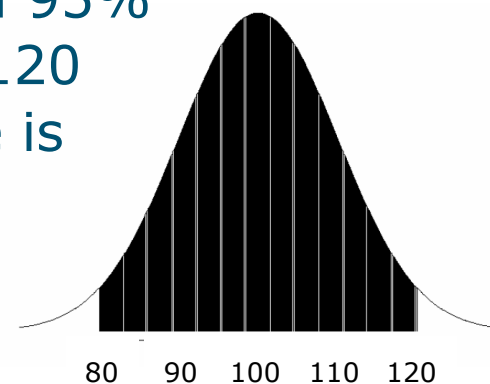
- Systematic errors are to be avoided where possible , or quantified ex-post and removed.
- Uncertainties that stem from random errors tend to cancel out each other at higher levels of aggregation. For example, estimates at national levels (e.g., total biomass, total forest area) *usually** have a lower impact from random errors than estimates at regional levels.

*Assuming that larger areas have greater sample sizes which, in turn, lead to greater precision and less uncertainty. However, for a smaller area and a larger area with the same sample size, the smaller area would probably have greater precision and less uncertainty, because the smaller area is likely more homogeneous. Thus sample size, and not the size of the area, is important.



95% Confidence interval

- Uncertainty is usually expressed by a 95% *confidence interval*:
 - 95% of confidence intervals constructed using samples obtained with the same sampling design will include the true value.
 - If the area of forest land converted to cropland (mean value) is 100 ha, with a 95% confidence interval ranging from 80 to 120 ha, the uncertainty in the area estimate is $\pm 20\%$.
 - The 2.5th percentile is 80 and the 97.5th percentile is 120.



Source: IPCC GPGULUCF



Correlation

- *Correlation* means dependency between parameters:
 - The “Pearson correlation coefficient” assumes values between $[-1, +1]$
 - Correlation coefficient of $+1$ means a perfect positive correlation
 - If the variables are independent of each other, the correlation coefficient is 0



Trend uncertainty

- The *trend* describes the change of emissions or removals between two points in time.
- *Trend uncertainty* describes the uncertainty in the change of emissions or removals. Trend uncertainty is sensitive to the correlation between parameter estimates used to estimate emissions or removals for two points in time.
- Trend uncertainty is expressed as percentage points. For example, if the trend is +5% and the 95% confidence interval of the trend is +3 to +7%, we can say that trend uncertainty is $\pm 2\%$ points.



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Uncertainties in area changes

- In REDD+ context, an estimate of area and/or area change typically results from analysis of a remote-sensing-based map.
- Such maps are subject to classification errors that induce bias into estimations.
- A suitable approach is to **assess the accuracy of the map** and use the results of the accuracy assessment to adjust the area estimates.
- Most image classification methods have parameters that can be tuned to reduce uncertainties. A good tuning reduces bias, but has a certain degree of subjectivity.



Accuracy assessment of land cover and changes (1/4)

Use of accuracy assessment results for area estimation

- The aim of the accuracy assessment is to characterize the frequency of errors (omission and commission) for each land cover class.
- Differences in these two errors may be used to adjust area estimates and also to estimate the uncertainties (confidence intervals) for the areas for each class.
- Adjusting area estimates on the basis of a rigorous accuracy assessment represents an improvement over simply reporting the areas of map classes.



Accuracy assessment of land cover and changes (2/4)

- For **land-cover** maps the accuracy of remote sensing data (single-date) may be assessed with widely accepted methods.
- These methods involve assessing the accuracy of a map using *independent reference data* (of greater quality than the map) to obtain—by land-cover class or by region—the *overall accuracy*, and:
 - *Errors of omission* (excluding an area from a category to which it does truly belong, i.e., area underestimation)
 - *Errors of commission* (including an area in a category to which it does not truly belong, i.e., area overestimation)



Accuracy assessment of land cover and changes (3/4)

■ Example of accuracy measures for the forest class:

- Error of commission: $(13+45)/293 = 19.80\%$
- Error of omission: $(25+3)/263 = 10.65\%$
- User's accuracy: $235/293 = 80.20\%$
- Producer's accuracy: $235/263 = 89.35\%$

■ Overall accuracy = $(235+187+215+92+75)/986 = 81.54\%$

	Reference data					
Class. data	F	A	W	U	B	Total
F	235	13	0	45	0	293
A	25	187	7	18	20	257
W	3	0	215	0	0	218
U	0	0	0	92	35	127
B	0	0	0	16	75	91
Total	263	200	222	171	130	986



Accuracy assessment of land cover and changes (4/4)

For **land-cover changes**, additional considerations apply:

- It is usually more difficult to obtain suitable, multitemporal reference data of greater quality to use as the basis of the accuracy assessment, particularly for historical time frames.
- Since the changed classes are often small proportions of landscapes, it is easier to assess errors of commission (by examining small areas identified as changed) than errors of omission (by examining large area identified as unchanged).
- Other errors such as geo-location of multitemporal datasets and inconsistencies in processing/analysis and in cartographic/thematic standards are exaggerated and more frequent in change assessments.



Sources of uncertainty

Different components of the monitoring system affect the quality of the estimates, including:

- Quality and suitability of satellite data (i.e., in terms of spatial, spectral, and temporal resolution)
- Radiometric / geometric preprocessing (correct geolocation)
- Cartographic standards (i.e., land category definitions and MMU)
- Interpretation procedure (algorithm or visual interpretation)
- Postprocessing of the map products (i.e., dealing with no data, conversions, integration with different data formats)
- Availability of reference data (e.g., ground truth data) for evaluation and calibration of the system



Addressing sources of uncertainty

Many of these sources of uncertainty can be addressed using widely accepted data and approaches:

- Suitable of satellite data: Landsat-type data, for example, have been proven useful for national-scale land cover changes for MMU of 1 ha
- Data quality: suitable preprocessing for most regions provided by some data providers (i.e., global Landsat Geocover)
- Consistent and transparent mapping: same cartographic and thematic standards and accepted interpretation methods should be applied transparently using expert interpreters

The accuracy assessment should provide measures of thematic accuracy and confidence intervals for estimates of activity data



Errors in area-change estimates: Example

Why errors in area-change estimates are more frequent than errors in area estimates

Map at time 1



Map at time 2



Overlap (change)



- Omission error (forest reported as nonforest)
- Commission error (nonforest reported as forest)
- False afforestation
- False deforestation



Constructing area-change maps

Two general approaches for constructing area-change maps:

- **Direct classification** entails construction of the map directly from a set of change training data and two or more sets of remotely sensed data. If it is possible, this is often preferred, also because it has only a single set of errors
- **Postclassification** entails construction of the map by comparing two separate land-cover maps, each constructed using single sets of land-cover training data and remotely sensed data. Often it is the only possible alternative because of the inability to observe the same locations on multiple occasions as is required to obtain change training data, insufficient numbers of change training observations, or a requirement to use an historical baseline map.



Reference data and training data

- *Reference data* should be distinguished from the *training data*.
- If estimates of accuracy, land cover, or change are to be representative of entire areas of interest, the reference data must be acquired using a probability sampling design.
- The nature of the reference data depends on the method used to construct the map:
 - For maps constructed using direct classification, the reference data must consist of observations of change based on two dates for the same sample locations.
 - For maps constructed using postclassification, reference data may consist of either the same reference data as for maps constructed using direct classification or for two dates, each at different locations.



Elements for a robust accuracy assessment

For robust accuracy assessment of land cover or land-cover change maps and estimates, statistically rigorous validations include three components:

- Sampling design
- Response design
- Analysis design



Sampling design

- Protocol for **selecting the locations** at which the **reference data** are obtained: It includes specification of the *sample size*, *sample locations*, and *the reference assessment units* (i.e., pixels or image blocks).
- Stratified sampling should be used for rare classes (e.g., change categories).
- Systematic sampling with a random starting point is generally more efficient than simple random sampling and is also more traceable.



Response design

- Protocols used to **determine the reference or ground condition classes** and the definition of agreement for comparing the map classes to the reference classes.
- Reference information should come from data of greater quality than the map labels; ground observations are generally considered the standard, although finer resolution remotely sensed data are also used.
- Consistency and compatibility in thematic definitions and interpretation are required to compare reference and map data.



Analysis design

- It includes **estimators** (statistical formulas) and **analysis procedures for accuracy estimation and reporting**.
The estimators must be consistent with the sampling design.
- Comparisons of map and reference data produce a suite of statistical estimates including *error matrices*, *class-specific accuracies* (of commission and omission error), *area and area-change estimates*, and associated *variances and confidence intervals*.



Considerations for implementation and reporting

- The techniques described rely on probability sampling designs and the availability of suitable reference data.
 - Such approach may not be achievable, in particular for historical land changes.
- In the early stages of developing a national monitoring system, the verification efforts should help to build confidence.
 - Greater experience (i.e., improving knowledge of source and magnitude of potential errors) will help reducing the uncertainties.
- If no accuracy assessment is possible, it is recommended to perform, as a minimum, a *consistency assessment* (i.e., reinterpretation of small samples in an independent manner) which may provide information of the quality of the estimates.



Building confidence in estimates

Information obtained without a proper probability sample design can still be useful to build confidence in the estimates, e.g.:

- Spatially-distributed confidence values provided by the interpretation
- Systematic qualitative examinations of the map and comparisons (qualitative / quantitative) with other maps
- Review by local and regional experts
- Comparisons with non-spatial and statistical data

Any uncertainty bound should be treated conservatively to avoid producing a benefit for the country (overestimation of removals or of emissions reductions)



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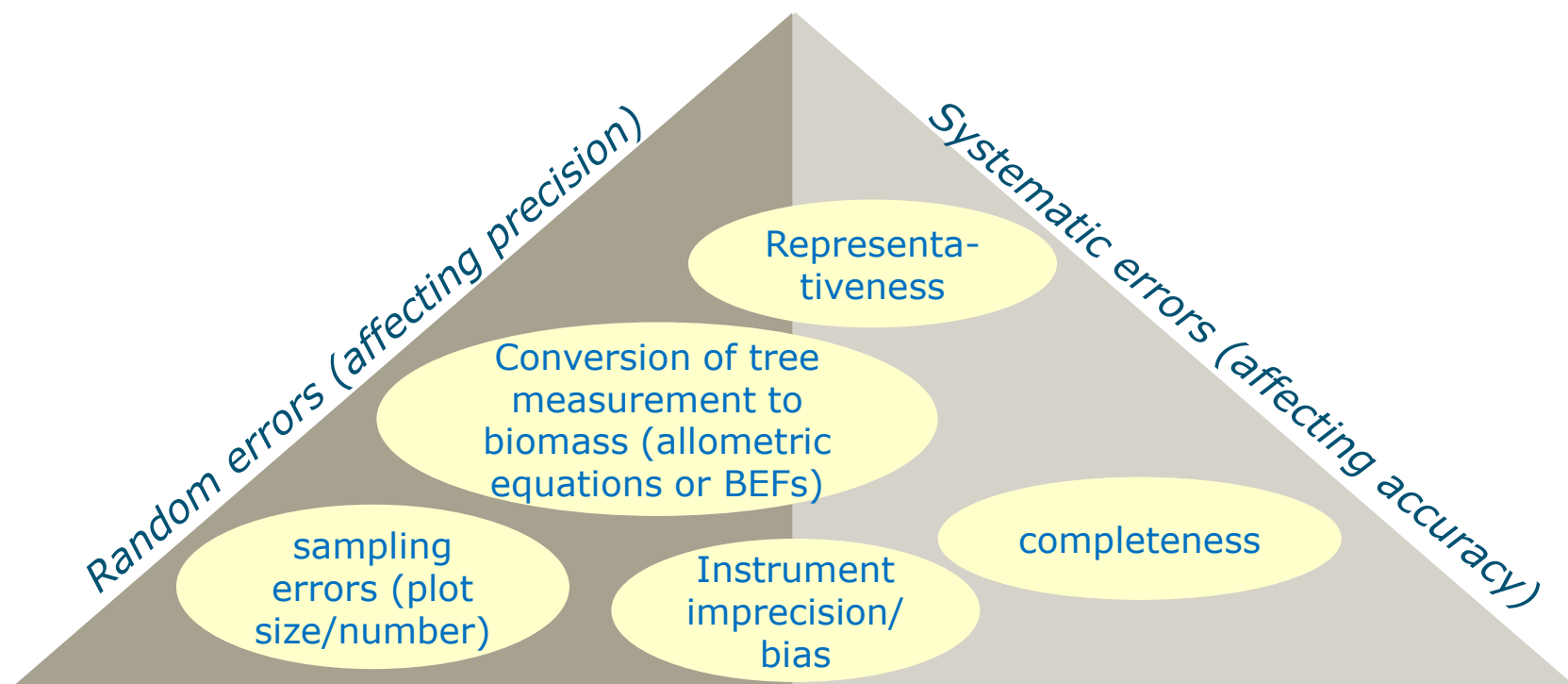
Uncertainties in carbon stock changes

- Assessing uncertainties of the estimates of C stocks and C stocks changes is usually more challenging (and often subjective) than estimating uncertainties of the area and area changes
- According to the literature, the overall uncertainty for C stocks estimates is usually larger than the uncertainty for area estimates. However, when looking at changes (i.e. trends) in C stocks and areas, the picture *may* change, depending on possible correlation of errors (see later)



Random errors and systematic errors

- Uncertainty of carbon stocks can be caused by both *random errors* and *systematic errors*, but sometimes it may be difficult to distinguish between the two.



Uncertainties due to random errors

- *Instrumental imprecision* (noise, wrong handling, etc.)
- *Sampling errors* (i.e., plot size and number), common with high natural variation of biomass in tropical forests



Biomass depends on temperature, precipitation, forest type and species, stratification, spatial scale, natural and human disturbances, soil type, and soil nutrients.



Conversion of tree measurement to biomass

- Allometric model or biomass expansion factors (BEFs):
 - Selection of best-fitting allometric model for respective forest type → \approx 20% error of tree AGB estimate
- Overall:
 - Uncertainties on plot level (at 95% CI*): 5% to 30%
 - Average range of AGB of IPCC: -60% to +70%

*CI = confidence interval.



Dealing with uncertainties due to random errors

- If feasible: increase sample size (maybe problematic)
- High tree biodiversity → regional/pan-tropical allometric models are better than site-specific models (error $\pm 5\%$)

Dry forest stands:

$$- AGB = \exp(-2.187 + 0.916 \times \ln(pD^2H)) \equiv 0.112 \times (pD^2H)^{0.916}$$

$$- AGB = p \times \exp(-0.667 + 1.784\ln(D) + 0.207(\ln(D))^2 - 0.0281(\ln(D))^3)$$

Having H (height), estimates are more accurate

Moist forest stands:

$$- AGB = \exp(-2.977 + \ln(pD^2H)) \equiv 0.0509 \times pD^2H$$

$$- AGB = p \times \exp(-1.499 + 2.148\ln(D) + 0.207(\ln(D))^2 - 0.0281(\ln(D))^3)$$

Equations from Chave et al., 2005



Further regional/pan-tropical allometric models

■ (error $\pm 5\%$)

Moist mangrove forest stands:

- $AGB = \exp(-2.977 + \ln(pD^2H)) \equiv 0.0509 \times pD^2H$

- $AGB = p \times \exp(-1.349 + 1.980\ln(D) + 0.207(\ln(D))^2 - 0.0281(\ln(D))^3)$

Wet forest stands:

- $AGB = \exp(-2.557 + 0.940 \times \ln(pD^2H)) \equiv 0.0776 \times (pD^2H)^{0.940}$

- $AGB = p \times \exp(-1.239 + 1.980\ln(D) + 0.207(\ln(D))^2 - 0.0281(\ln(D))^3)$

AGB = aboveground biomass in kg; D = diameter in cm; p = oven-dry wood over green volume in g/cm⁻³; H = height of tree in m; \equiv = mathematical identity



Uncertainties due to systematic errors

- *Completeness of carbon pools:* aboveground biomass, belowground biomass, soil organic carbon, deadwood, litter:
 - Literature suggests that for deforestation, $\approx 15\%$ of emissions may come from dead organic and $\approx 25\text{--}30\%$ may come from soils (more if organic soils)
 - However, these pools are often not included when calculating emission factors, due to lack of data



Dealing with uncertainties due to carbon pool completeness

- All “*significant*” pools and activities should be included:
 - First, “*Key categories*” (KC) (i.e., categories/ activities contributing substantially to the national GHG inventory) should be identified following IPCC guidance (IPCC, 2006, V4, Ch1.1.3)
 - Within a KC, a pool is “significant” if it accounts for >25-30% of emissions from the category
- Pools may be omitted under principle of *conservativeness*
- Furthermore, emissions/removals from KC and significant pools should be estimated with Tier 2 or 3 methods,* which are assumed less uncertain than tier 1

*National circumstances (e.g., documented lack of resources) may justify use of Tier 1 for KC



Representativeness of the sampling plots

- *High variation of biomass content within tropical forests
→ a nonrepresentative sample may introduce a significant bias*



Dealing with uncertainties due to representativeness

- Sound statistical sampling necessary in “hotspots”
- Distribution of samples across major soil/topographic gradients of landscape, e.g., 20 plots (each 0.25ha) or one sample of 5ha may allow landscape-scale AGB estimation with $\pm 10\%$ (95% CI)
- If geographic position known, global biomass maps (1km Saatchi / 500m Baccini) can be used for estimating AGB
- If geographic position unknown, global biomass maps can be used to derive improved Tier 1 data values



Error propagation of AGB estimation

For Central Panama:

(Chave et al. 2004)

Table 3. Summary of the sources of error in the AGB estimation of a tropical forest.

(Type 1 error refers to the error made in the estimation of the AGB held in a single tree; this error averages out in plots. Type 2 error is that caused by the choice of the allometric model. Types 3 and 4 are two types of sampling error, which can be minimized by large-sized, multi-plot, censuses. The reported values are examples for the forests of the Panama Canal watershed.)

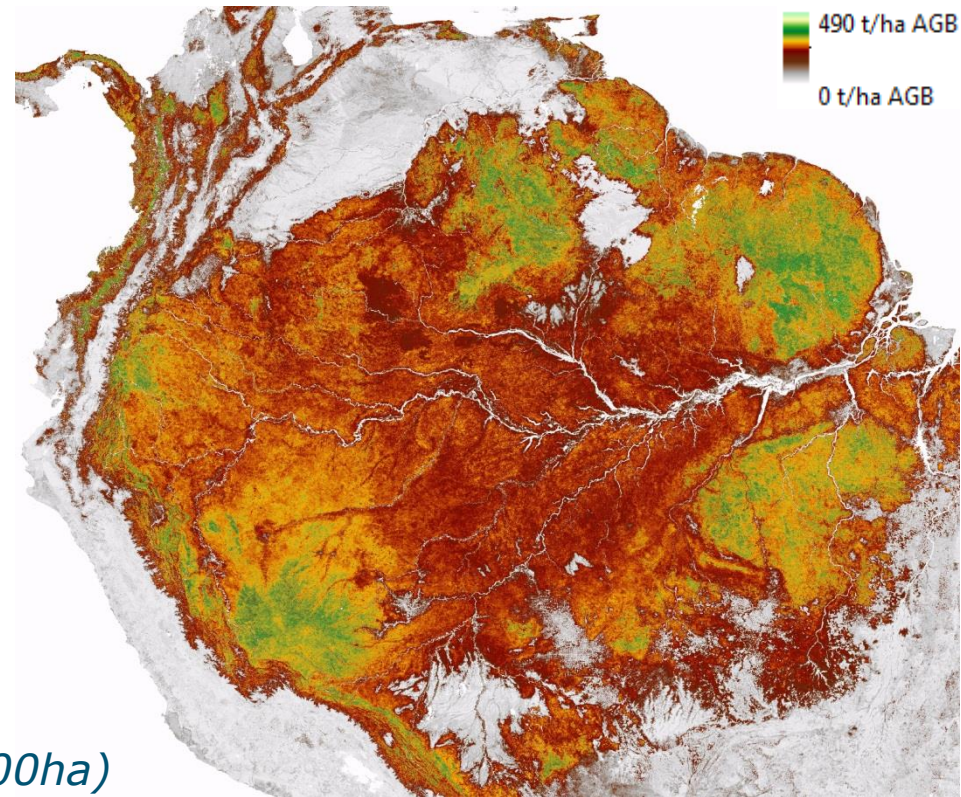
error type		s.e.m. (percentage of the mean)	type of data
1. tree level error	trees > 10 cm diameter	48	BCI plot—pan-tropical allometric model
	trees < 10 cm diameter	78	
2. allometric model	before ρ correction	22	BCI plot—eight allometric models
	after ρ correction (gravity)	13	
	after large tree correction	11	
3. within-plot uncertainty	0.1 ha plot	16	BCI plot—pan-tropical allometric model
	0.25 ha plot	10	
	1 ha plot	5	
4. among-plot uncertainty		11	Marena plots—pan-tropical allometric model
total	50 1 ha plots, after ρ and large tree corrections	24	—



Examples of uncertainties of recent AGB global maps (1/3)

Saatchi map at 95% CI:

- *Overall AGB uncertainty at pixel-level (averaged)*
 $\pm 30\%$ ($\pm 6\%$ to $\pm 53\%$)
- *Regional uncertainties:*
America $\pm 27\%$; Africa $\pm 32\%$
Asia $\pm 33\%$
- *Total C stock uncertainty at pixel-level (averaged)*
 $\pm 38\%$;
 $\pm 5\%$ (10,000ha); $\pm 1\%$ ($>1,000,000\text{ha}$)



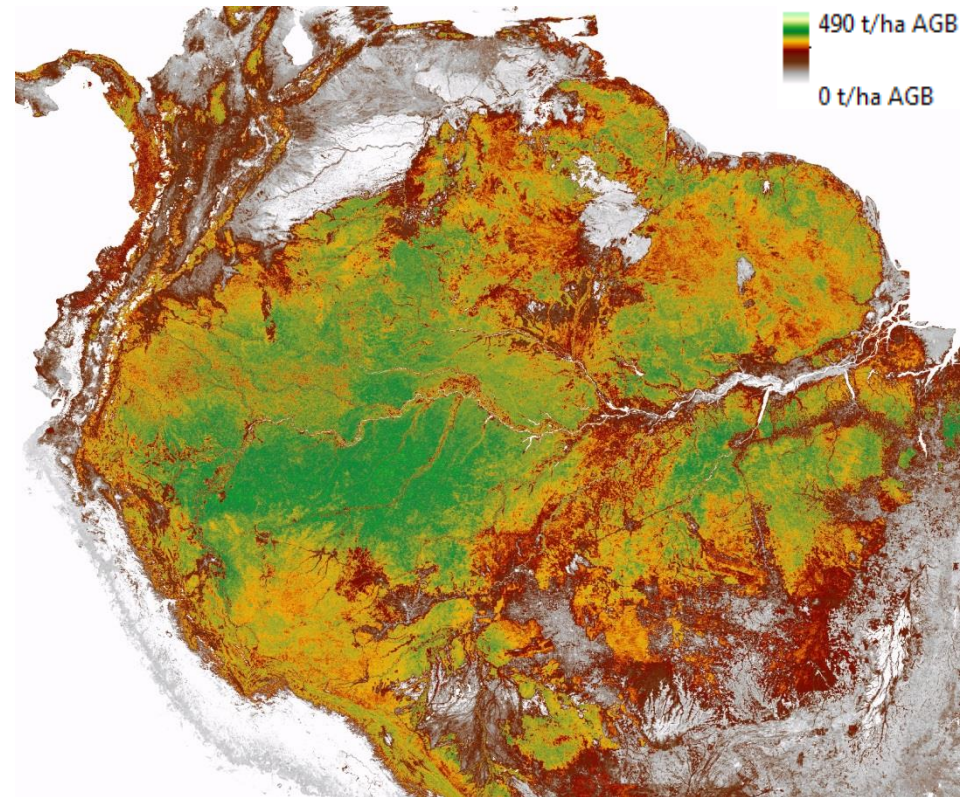
Examples of uncertainties of recent AGB global maps (2/3)

Baccini map at 95% CI:

■ *Regional uncertainties for carbon stocks:*

America $\pm 7.1\%$; Africa $\pm 13.2\%$

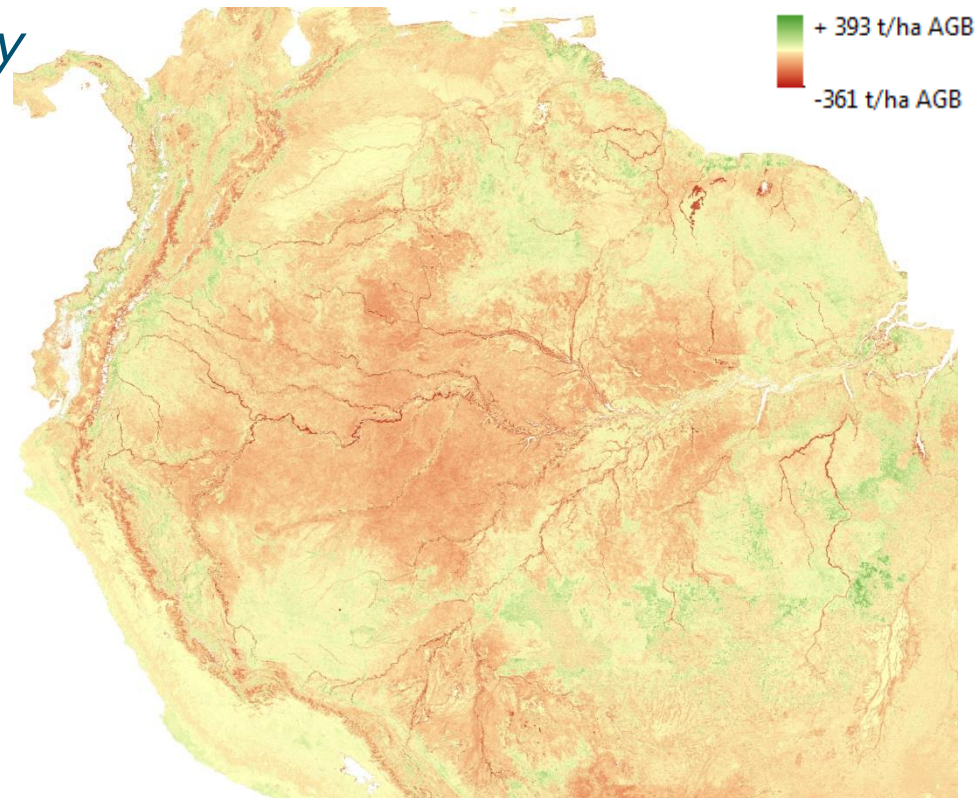
Asia $\pm 6.5\%$



Examples of uncertainties of recent AGB global maps (3/3)

Difference between Baccini and Saatchi maps:

- *Recent analysis shows locally significant differences, but at region-scale level results are comparable*



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Combination of uncertainties

- The uncertainties in individual parameters can be combined using either:
 - *Error propagation* (IPCC Tier 1), which is easy to implement using a spreadsheet tool; certain conditions have to be fulfilled so that it can be used.
 - *Monte Carlo simulation* (IPCC Tier 2), based on modelling and requiring more resources to be implemented; it can be applied to any data or model.



Tier 1 level assessment (1/3)

Tier 1 should preferably be used only when:

- Estimation of emissions and removals is based on addition, subtraction, and multiplication
- There are no correlations across categories (or categories are aggregated in a way that correlations are unimportant)
- Relative ranges of uncertainty in the emission factors and area estimates are the same in years 1 and 2
- No parameter has an uncertainty $>$ than about $\pm 60\%$
- Uncertainties are symmetric and follow normal distribution

Even in the case that not all of the conditions are fulfilled, the Tier 1 method can be used to obtain approximate results

If asymmetric distributions \rightarrow take higher absolute value



Tier 1 level assessment (2/3)

■ Equation for multiplication:

$$U_{total} = \sqrt{U_1^2 + U_2^2 + \dots + U_n^2}$$

Where:

U_i = percentage uncertainty associated with each of the parameters

U_{total} = the percentage uncertainty in the product of the parameters

■ Equation for addition

$$U_{total} = \frac{\sqrt{(U_1 * x_1)^2 + (U_2 * x_2)^2 \dots (U_n * x_n)^2}}{|x_1 + x_2 \dots + x_n|}$$

and subtraction:

Where:

U_i = percentage uncertainty associated with each of the parameters

x_i = the value of the parameter

U_{total} = the percentage uncertainty in the sum of the parameters



Tier 1 level assessment (3/3)

Examples of combination of uncertainties with Tier 1

Multiplication

	Mean value	Uncertainty (% of the mean)
Area change (ha)	10827	8
Carbon stock (t C/ha)	148	15

Thus the total carbon stock loss over the stratum is:
 $10,827 \text{ ha} * 148 \text{ tC/ha} = 1,602,396 \text{ t C}$

And the uncertainty = $\sqrt{8^2 + 15^2} = \pm 17\%$

Addition

	Mean	95 % CI
	t (C/ha)	
Living Trees	113	11
Down Dead Wood	18	3
Litter	7	2

therefore the total stock is 138 t C/ha and the uncertainty =

$$\frac{\sqrt{(11\% * 113)^2 + (3\% * 18)^2 + (2\% * 7)^2}}{|113 + 18 + 7|} = \pm 9\%$$

The total uncertainty is $\pm 9\%$ of the mean total C stock of 138 t C/ha



Tier 1 trend assessment (1/2)

Estimation of trend uncertainty (Tier 1) is based on the use of two sensitivities:

- Type A sensitivity, which arises from uncertainties that affect emissions or removals in the years 1 and 2 equally (i.e., the variables are correlated across the years)
- Type B sensitivity, which arises from uncertainties that affect emissions or removals in the year 1 or 2 only (i.e., variables are uncorrelated across the years)

Basic assumption: *EF fully correlated across the years* (Type A sensitivity), *AD uncorrelated across years* (Type B sensitivity)



Tier 1 trend assessment (2/2)

Table to combine level and trend uncertainties using Tier 1

A	B	C	D	E	F	G	H	I	J	K	L	M
Category	Gas	Emissions or removals in year 1	Emissions or removals in year 2	Area uncertainty	Emission factor uncertainty	Combined uncertainty	Contribution to variance by category in year 2	Type A sensitivity	Type B sensitivity	Uncertainty in trend by introduced emission factor uncertainty (Note ii)	Uncertainty in trend by area introduced by area uncertainty (Note iii)	Uncertainty introduced to the trend in total emissions/
		Mg CO ₂	Mg CO ₂	%	%	$\sqrt{E^2 + F^2}$	$\frac{(G * D)^2}{(\sum D)^2}$	Note i	$\frac{D}{\sum C}$	$I * F$	$J * E * \sqrt{2}$	$K^2 + L^2$
E.g. Forest converted to Cropland	CO ₂											
E.g. Forest converted to Grassland	CO ₂											
Etc	...											
Total		$\sum C$	$\sum D$				$\sum H$					$\sum M$
					Level uncertainty		$\sqrt{\sum H}$				Trend uncertainty	$\sqrt{\sum M}$

Tier 1 trend assessment and calculation of total uncertainty can be carried out using this table.

See GOFC-GOLDC (2014) *Sourcebook*, section 2.7, for explanation of notes.

Tier 2 level assessment: Monte Carlo simulation (1/2)

Tier 2 method is based on a **Monte Carlo simulation**:

- Tier 2 method can be applied to any equation (whereas Tier 1 is applicable only for addition, subtraction, and multiplication). Tier 2 can also be applied to entire models.
- Tier 2 gives more reliable results than Tier 1, particularly where uncertainties are large, distributions are non-normal, or correlations exist.
- Application of Tier 2 requires programming or use of a statistical software package.
- For more details, see IPCC (2003, ch. 5) guidance and IPCC (2006, vol. 1, ch. 3) guidelines.



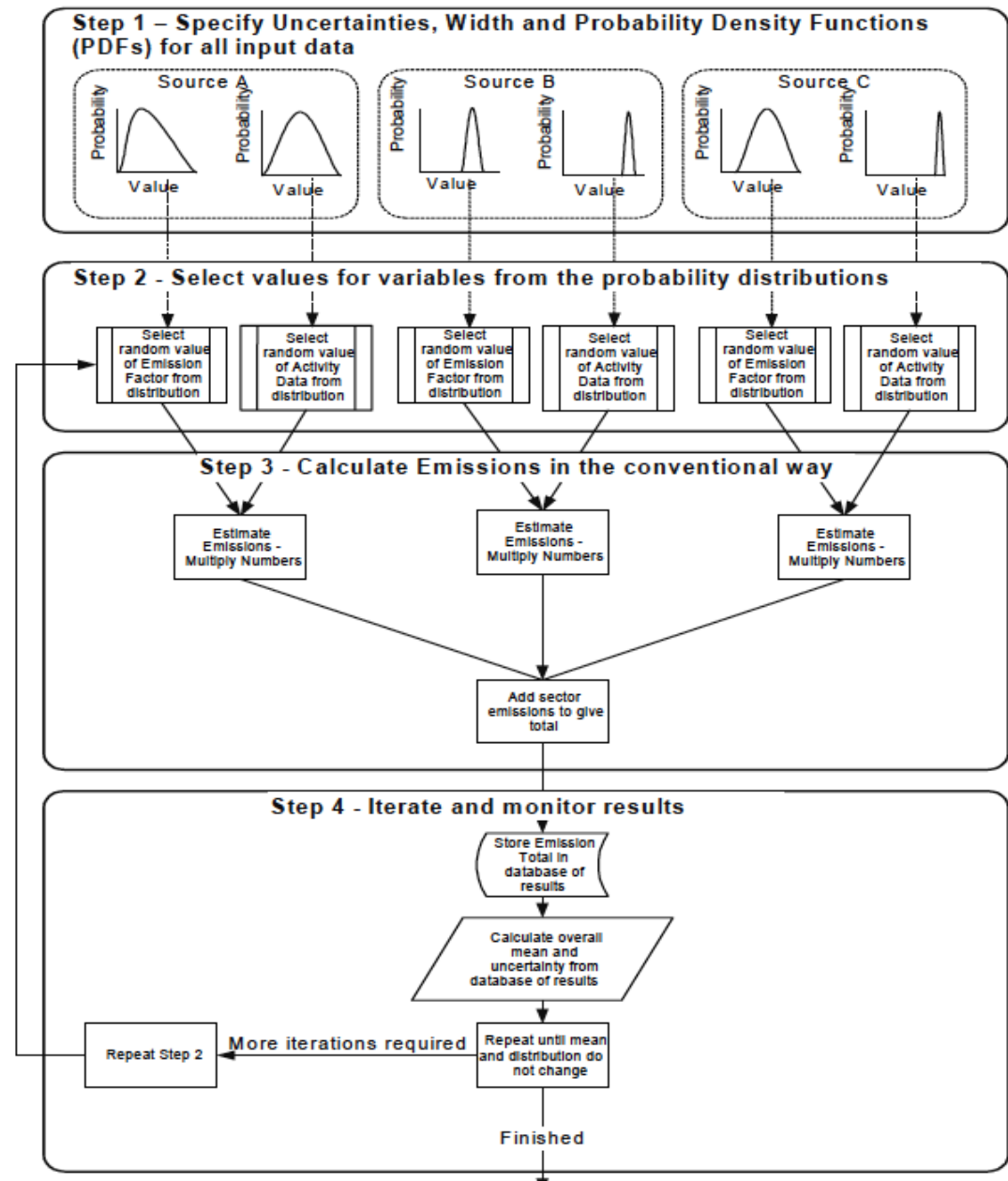
Tier 2 level assessment: Monte Carlo simulation (2/2)

- The principle of Monte Carlo analysis is to select *random values* of emission factor (EF), activity data (AD), and other estimation parameters from within their individual probability density functions and to calculate the corresponding emission values.
- This procedure is repeated many times (e.g., 5,000 or 10,000), using a computer. This yields 5,000 or 10,000 values for emission, based on which the user can calculate the mean value of emission and its 95% confidence interval.



Illustration of Monte Carlo method

Source: IPCC 2006, Ch. 3.

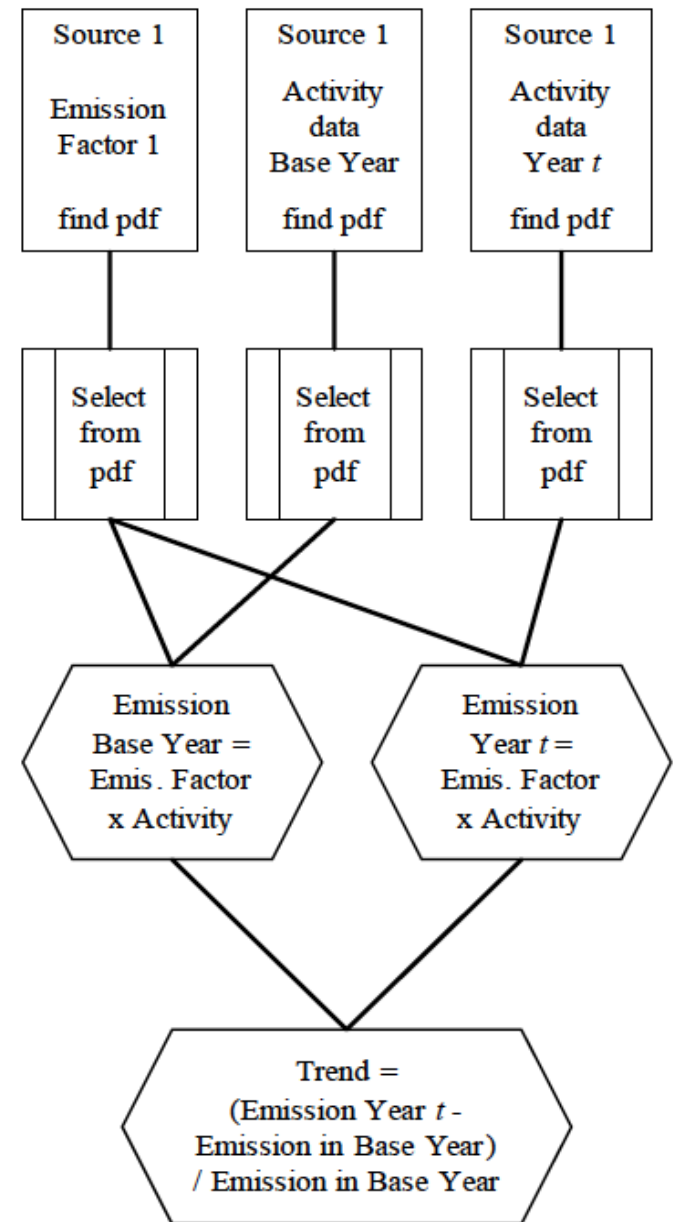


Calculation scheme for Monte Carlo analysis

Calculation scheme for Monte Carlo analysis of the **absolute emissions** and the **trend** of a single category, estimated as EF times an AD (IPCC 2006).

The figure shows the case where the EF is 100% correlated between base year and year t (e.g., the same emission factor is used in each year and there is no year to year variation expected)

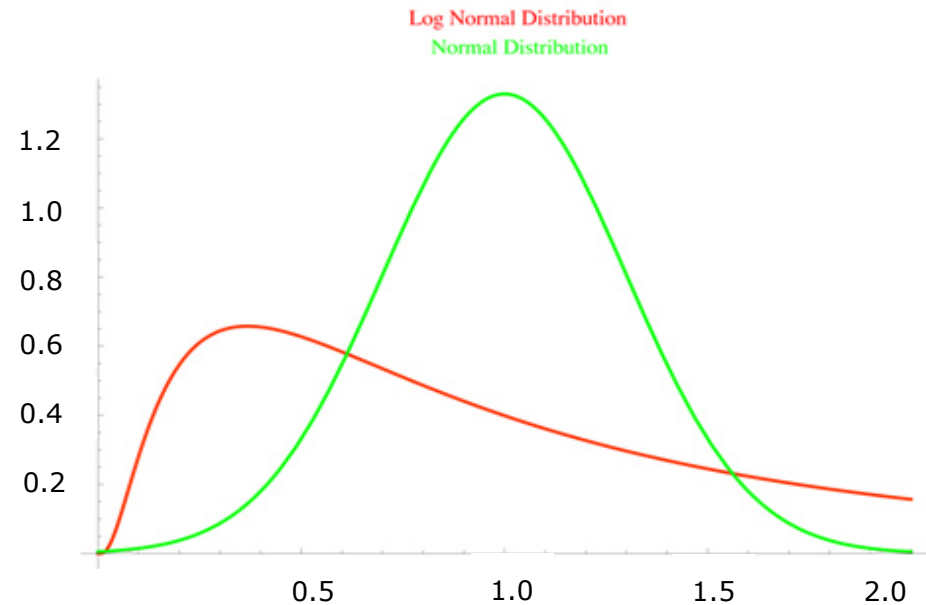
→ To see the case of uncorrelated EF, see IPCC (2006, vol. 1, ch. 3, fig. 3.7).



Data required to run Monte Carlo simulation

- *Uncertainty of each parameter expressed as probability density function*: Any distribution can be used with Monte Carlo. For simplicity (and if more detailed information is not available), symmetric uncertainties are often assumed to be *normally* distributed and positively skewed uncertainties *lognormally* distributed.

- *Correlations across parameters*: Monte Carlo simulation can deal with both full and partial correlations.



Reporting of uncertainties

Uncertainties should be reported with a standardized format

A	B	C	D	E	F	G	H	I	J
Category	Gas	or Emissions removals in year 1	or Emissions removals in year 2	Area uncertainty	Emission factor uncertainty	Combined uncertainty	Inventory trend for year 2 increase with respect to year 1 (Note a)	Trend uncertainty of the category	Method used to estimate uncertainty (Note b)
		Mg CO ₂	Mg CO ₂	%	%	%	% of year 1		
E.g. Forest Land converted to Cropland	CO ₂								
E.g. Forest Land converted to Grassland	CO ₂								
Etc	...								
Total						Level uncertain ty		Trend uncertain ty	

See GOFD-GOLDC (2014, sect. 4) *Sourcebook* for explanation of notes.

In summary (1/2)

- Assessing uncertainty is fundamental in the IPCC and UNFCCC contexts.
- Uncertainty consists of two components: *systematic errors* and *random errors*.
- *Accuracy assessment* of land cover and changes is used to characterize the frequency of errors (omission and commission) for each class and the overall accuracy of the map using an independent reference dataset.



In summary (2/2)

- Assessing uncertainties of the estimates of C stocks and C stocks changes is usually more challenging due to different types of random and systematic errors.
- The uncertainties in individual parameters can be combined using either error propagation (Tier 1) or Monte Carlo analysis (Tier 2).



Country examples and exercises

Country examples

1. Biomass burning
2. Uncertainty analysis: LULUCF in Finland
3. Applying the conservativeness approach to the DRC example (matrix approach) - **See also Exercise 4**

Exercises

1. Uncertainties in area and area change
2. Using IPCC equations to combine uncertainties
3. Using IPCC equations to assess trend uncertainties
4. The REDD+ matrix approach (see xls exercise file and country example – this exercise is **in common with Module 3.3**)
5. Preparations for Monte Carlo



Recommended modules as follow up

- **Module 2.8** to learn more about the role of evolving technologies for monitoring of forest area changes and changes in forest carbon stocks
- Modules **3.1 to 3.3** to proceed with REDD+ assessment and reporting



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